



## ANALYSIS OF RAIN RATE AND RAIN ATTENUATION FOR EARTH-SPACE COMMUNICATION LINKS OVER UYO - AKWA IBOM STATE

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### ABSTRACT

*Rain rate and rain attenuation predictions are vital when designing microwave satellite and terrestrial communication links, such as in the Ku and Ka bands. This paper presents the cumulative distribution functions (CDFs) of the predicted rain rate and rain attenuation for Uyo, Akwa Ibom State (AKS) (Latitude: 4.88°N, Longitude: 8.09°E, Height above Sea Level: 51.2 m), a typical rain forest zone in Nigeria, using rainfall data for three years spanning between January 2010 and December 2012. These measurements were recorded by the meteorology department of the Akwa Ibom International Airport (AIIA), Uyo for percentage availabilities 99.9 to 99.999. Rain-rate measurements were carried out using the Moupfouma and Chebil models – models purposely designed for tropical zones, while the International Telecommunications Union Radio-wave propagation (ITU-R P) models were used for estimating rain-attenuation. The results obtained will serve as a good preliminary design tool for both terrestrial and earth-satellite microwave links.*

**Keywords:** Rain Rate, Rain Attenuation, Propagation Impairment, Cumulative Distribution.

### 1. INTRODUCTION

The presence of rain along satellite-earth path is a major cause of signal attenuation at frequencies above 10 GHz [1]. Raindrops absorb and scatter radio waves, resulting in signal attenuation, and in the reduction of the overall link availability. The severity of rain impairment increases with frequency, and varies with climates[2]. It is therefore very important when planning both microwave satellite and terrestrial line-of-sight links, to make an accurate prediction of rain induced attenuation [3]. Initially, attenuation prediction attempts involved extrapolation of rain attenuation measurements from specific locations to other locations using frequencies (frequency scaling), or elevation angles (elevation scaling) in [4]; however, the complex nature and regional variability of rainfall distributions make this approach highly inaccurate[5]. Several procedures exist for the prediction of rain attenuation on earth-space paths. These procedures can be grouped in two classes: empirical and physical. Empirical classes are based on measurement databases from stations in different locations within a given region; and physical classes attempt to

reproduce the physical behaviour involved in the attenuation process [6].

Empirical method is more frequently used. It makes use of equations with variables, such as rain height, rain rate and earth-station latitude and longitude [1]. In empirical method, an appropriate distribution of rainfall rate at 1-minute integration time is needed for the site under study in order to predict accurately the rain attenuation for that location[7]. This is because rain rates obtained through longer periods of integration might fail to capture a high-intensity, short-duration rain event, and are not recommended for communication systems designs[1].

### 2. REVIEW OF RELATED WORKS

A few research works have so far been carried out to obtain a rainfall rate of 1-minute integration time necessary for the study of rain induced impairments of propagation signals, especially in a tropical country such as Nigeria. The locations in Nigeria (mostly in the South West) where results have been obtained previously include Ile-Ife, Osun State [8], Akure, Ondo State [9-11], Ota, Ogun State [12], Ogbomosho, Oyo State [13], Ilorin, Kwara State [14].

The rain in Nigeria is characterized by high intensity rainfall, high frequency of rain occurrence and the increased presence of large raindrops when compared with temperate climates[7]. The data used for these analyses were obtained from the Tropical Rain Measurement Mission (TRMM) jointly developed by the United States of America (USA) and Japan, and also from the Global Precipitation Climatology Project (GPCP) on the World Climatic Research Programme (WCRP). However, these data cannot be employed directly in system design, due to its long integration time. Hence, methods that convert the available rain rate data to the equivalent 1-minute rain rate cumulative distribution is necessary for the accurate prediction of rain rate, such methods include the ITU-R[15]and model Crane Model [16] for rain-rate prediction. This paper presents estimates of rainfall rates at 0.001 to 0.1% of the time exceeded for an average year, and uses these values to estimate rain attenuation of microwave signals on earth-space path, and then make comparisons with the prediction in [15].

Rain-rate and rain-attenuation prediction have naturally attracted a great deal of attention as in research works carried out in the USA[17], Malaysia[18], Colombia [1],Nigeria [7, 19, 20]and on a global scale [3, 21].The rainfall rates rain attenuation at 0.001 to 0.1% of time exceeded for an average year and rain attenuation for AKS were obtained using Moupfouma [22] and Chebil [18] models designed for tropical zones. These models are a mix of the log-normal distribution of low rain rates and the gamma distribution for high rain rates, and ITU model for predicting rain attenuation [4].

Furthermore, efforts have been made by Ajayi and Ezekpo [23] and Omotosho and Oluwafemi [19]to obtain 1-minute rain rate map, and rain rate estimation respectively for Nigeria, using Rice-Holmberg (R-H) model. The model is best behaved over the distribution, while the Moupfouma model performs suitably well, according to Ojo in [7]. Results for the rain rate exceeded for 0.01% of the time agrees with estimates for the cumulative rain rate distribution derived from higher integration-time statistics over this tropical site.

### 3. RAIN RATE MODELS

The point rain rate is the rain rate measured at a point using a single rain gauge, as opposed to being measured over the entire link. A procedure for the calculation of a cumulative rain-attenuation

distribution from a point rain-rate distribution is therefore required if predictions are to be made. Several models exist that provide an estimation of the point rainfall-rate cumulative distribution.

Rice and Holmberg developed a model for obtaining rain rate values, after an analysis performed on measurements from stations inside and outside the USA, using the cumulative distributions of rain and maximum monthly period[24]. The result of the study is a point rain-rate cumulative rainfall accumulation, and a map of the highest rates expected for diurnal distribution based on a set of parameters obtained from the analysis of local rain accumulation data. Parameters include: the number of thunderstorm days expected in an average year 'U'; the highest monthly precipitation observed in a set  $M_m$ ; and the average annual accumulation M. The values of U and  $M_m$ , are averaged over a 30-year period. This model has a universal acceptability, because it is based on local data. It uses long-integration-time of local rainfall data to determine the CDF of rain rates [1].

However, the rain rate distribution is better described by the model in[22]to be log-normally distributed at the low rain rates, and a gamma distribution at high rain rates. The model is best for both tropical and temperate climates, and can be expressed by Equation (1) as:

$$P(R \geq r) = 10^{-4} \left( \frac{R_{0.01}}{r+1} \right)^b e^{(u[R_{0.01}-r])} \quad (1)$$

Where  $r$  (mm/h) represents the rain rate exceeded for a fraction of the time,  $R_{0.01}$  (mm/h) is the rain rate exceeded at 0.01 percent of time in an average year, and  $b$  is approximated by the expression in Equation (2):

$$b = \left( \frac{r - R_{0.01}}{R_{0.01}} \right) \ln \left( 1 + \frac{r}{R_{0.01}} \right) \quad (2)$$

The parameter  $u$  in Equation (1) governs the slope of the rain rate cumulative distribution, and depends on the local climatic conditions and geographical features. For tropical and sub-tropical localities,  $u$  is given in Equation (3) as

$$u = \frac{4 \ln 10}{R_{0.01}} e^{(-\lambda \left[ \frac{r}{R_{0.01}} \right]^\gamma)} \quad (3)$$

where  $\lambda = 1.066$  and  $\gamma = 0.214$ .

Thus, the Moupfouma model requires three parameters;  $\lambda$ ,  $\gamma$  and  $R_{0.01}$ . While the first two parameters  $\lambda$  and  $\gamma$ , have been provided.  $R_{0.01}$ , is estimated using the Chebil's model. This allows for the usage of long-time mean annual accumulation, M, at the location of interest.

The power law relationship of the model is given by Equation (4):

$$R_{0.01} = \alpha M^\beta \tag{4}$$

In (4),  $\alpha$  and  $\beta$  are regression coefficients defined as  $\alpha = 12.2903$  and  $\beta = 0.2973$ .

However, using the refined Moupfouma and Chebil model, the 1-minute rain-rate cumulative distribution can be fully determined from the long term mean annual rainfall data, and it is this model that is being used in this work, and then compared with the ITU model.

**4. RAIN ATTENUATION MODELS**

Ryde proposed a rain attenuation model in his paper published in [25], and cited in [26] three decades later. Crane applied measured data to Ryde’s model to evaluate the average matching between model predictions and measurements. Based on further analyses, Crane proposed a new revised model called two-component model[27].

The ITU rain attenuation prediction model[4] presents good results which have close proximity to the average prediction of a set of results obtained from the application of eight different methodologies[22]. Hence, this research work makes use of this model for rain attenuation prediction.

**5. AIIA DATA**

The rainfall data used for this research were obtained from the Meteorological Centre at the AIIA, Uyo. The

airport uses the tipping bucket range gauge, which is one of the meteorological measuring equipment connected to the Automatic Weather Observation System (AWOS) installed at the airport to obtain rainfall data. Rainfall data is automatically stored in two servers at a pre-determined time interval. Rainfall accumulation not up to a specified value in the interval measured was discarded. From these servers, the data is extracted into Microsoft Excel and that is what was obtained for processing. Three years of data spanning from January 2010 to December 2012 were recorded. The station parameters are latitude 4.88°N, longitude 8.09°E, and the height above sea level of 51.2m. A summary of the local climatology showing the rainfall accumulation at Uyo is presented in Table 1.

**6. ITU MODEL FOR POINT RAIN RATE DISTRIBUTION**

ITU-R recommendation P.837-6 [15] contains annexes and maps of meteorological parameters that have been obtained using the European Centre for Medium-Range Weather Forecast (ECMWF) ERA-40 re-analysis database, which are recommended for the prediction of rainfall rate statistics with a 1-minute integration time, when local measurements are not available. The model uses a database of parameters ( $\Pr_6$ ,  $M_t$  and  $\beta$ ), available from the ITU’s 3M Group[28], each of which is matched to a pair of longitude and latitude. This model was used to measure rain rate for comparison purposes and the result is presented in Figure 1.

*Table 1: Statistics of rainfall accumulation for Uyo from January 2010 to December 2012*

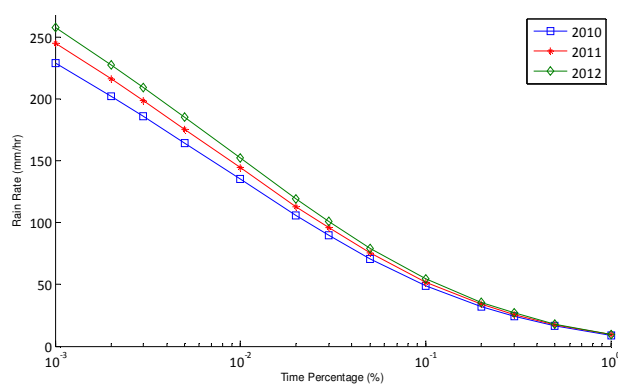
Month	2010		2011		2012	
	Total Volume of Rainfall Per Month in (mm)	No. of Rainy days	Total Volume of Rain Per Month in (mm)	No. of Rainy days	Total Volume of Rain Per Month in (mm)	No. of Rainy days
January	0.0	0	0.0	0	195.5	4
February	0.0	0	82.0	6	290.1	10
March	0.0	0	186.8	12	31.4	2
April	0.0	0	175.2	7	150.9	14
May	273.5	15	456.0	20	350.4	18
June	711.3	22	466.5	21	689.4	21
July	420.4	17	929.0	22	911.3	25
August	682.9	21	407.9	24	697.7	19
September	447.8	21	504.8	15	591.5	21
October	308.7	18	561.9	20	498.9	14
November	317.7	17	194.7	9	308.3	10
December	10.5	1	4.0	1	2.9	3
Total Volume of Rainfall per Year	3172.8	132	3968.8	157	4718.3	161

## 7. DEVELOPMENT OF POINT RAIN RATE DISTRIBUTION USING THE LOCAL CLIMATOLOGICAL DATA

The point rainfall rate for Uyo was obtained using Moupfouma model which approximates a log-normal distribution at the low rates, and a gamma distribution at high rain rate, was combined with the Chebil's model. Thus, by combining Equations (1) to (4) and using the parameters in Table 1 as inputs, a 1-minute rain-rate distribution shown in Figure 1 at 0.01% of time exceedance was obtained for each year. This is shown in Table 2.

*Table 2: Summary of Results for Rain Rate and Rain Attenuation (for 20 GHz) Estimates at 0.01% of Time Exceedance.*

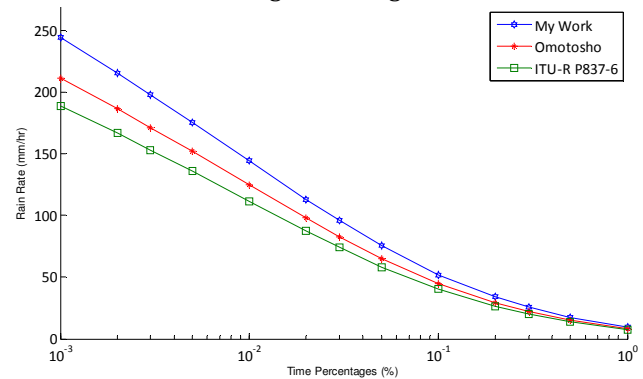
Year	2010	2011	2012	Average
Total Vol of rainfall (mm)	3172	3968	4718.3	3953.3
Number of rainy days	132	157	161	150
Rain rate (mm/hr)	135.06	144.36	151.98	144.19
Rain attenuation	46.62	48.44	49.89	48.41



*Figure 1: Cumulative rain rate distribution for Uyo for the years 2010 to 2012.*

From the results given in Table 2, it is seen that there has been a steady increase in rainfall accumulation for the three years under observation, which also inadvertently lead to a steady rise in rainfall rates. The average rainfall rate for Uyo is about 144mm/hr. Similar work carried out in Ajayi and Ezekpo [23] puts the rainfall rate for Uyo at 125mm/hr. Omotosho and Oluwafemi in [19] presented a value of 124mm/hr for Uyo. It should be noted that these two works were done with rain data collected over a 30-year period, and 9-year period respectively. The cumulative distribution shown in Figure 2 gives a comparison

between this research work, Omotosho and ITU-R P.837-6 model. The ITU model gives the lowest value of 111.5mm/hr. This is due to the fact that ITU measurements were carried out in temperate zones, hence give better performance within the temperate zones than in the tropics. A comparison performed with two years of rainfall data from Brazil concluded that the rain maps presented by ITU underestimated the rain rate cumulative distribution function for tropical zones[1]. According to Omotosho and Oluwafemi where locally measured data are not available, the ITU measurement may be used[19]. This is applicable only to the South West, South East, North West and North East regions of Nigeria.



*Figure 2: Comparison of rain rate distributions for Uyo*

Table 3 shows the percentage mean bias error of the derived 1-minute rainfall rates with other works. Hence, a comparison of the three research works in Figure 3 have similar results.

*Table 3: Percentage mean bias error of the derived 1-minute rainfall rates with other works*

ITU-RP837-6 mm/hr(A)	111.49	
Omotosho mm/hr (B)	124	
Ajayi-Ezekpo contour map data mm/hr (C)	125	
Present Work mm/hr (D)	144.19	
	(D - A)/D	22.7
% Mean Bias Error	(D - B)/D	14.0
	(D - C)/D	13.3

## 9. RAIN ATTENUATION DISTRIBUTION

Rain attenuation distribution was obtained using the ITU rain attenuation model[4, 29, 30]. The cumulative distributions of rain attenuation were evaluated for Ka band with frequency 20 GHz (downlink), elevation 54.5°, and a NIGCOMSAT 1-R orbital position of 42.5° E, in order to meet today's active challenges in the rapid growth of satellite broadband networks. The Ka-

band allows for a higher return link data rate. In order to obtain the rain attenuation at 0.001 to 0.1 percentage of the time exceeded, rain rate from each of the years in view, and the average rain rate was applied to the rain attenuation model in[4].

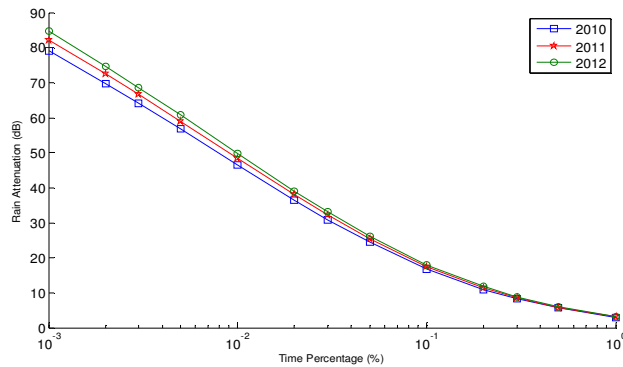


Figure 3: Cumulative Rain Attenuation Distribution for Uyo for the years 2010 to 2012.

Table 2 shows the average rain attenuation measured over Uyo to be approximately 48dB at a 0.01 % of time exceeded. The cumulative distributions of rain attenuation for the three years are shown in Figure 3. It is observed that, the value of the CDF of rain attenuation for the three years at 48dB may be considered very high for a system designer. However, this is seen to be consistent with the ITU which presents a measured value of about 41dB for the same location.

## 10. SEASONAL VARIATION OF RAIN RATE AND RAIN ATTENUATION

In Nigeria, there are two major seasons – the dry season (between December and May) and the wet season (between June and November). For the purpose of our analysis, the dry season was further subdivided into driest (December to February), and early rain (March to May) months. The wet season was subdivided into heavy rainfall (June to August) and moderate rainfall (September to November) months. Rainfall accumulation, rain rate and rain

attenuation for these seasons in each of the years were determined and the result is presented in Table 4.

From the result, as expected, rainfall accumulation was lowest between December and February for each of the three years: the year 2010 had the least rainfall by volume (10.5 mm), followed by 2012 (77.4 mm), while 2011 recorded the highest volume of rainfall (86.0 mm) for the driest months. The highest rainfall season was observed to be between June and August for all three years with rainfall accumulation as high as 2294 mm in 2012. The September to November season recorded moderately high rainfall volume for the three years.

The rain rate results also showed similar pattern. The lowest rain rate of 24.7 mm/hr was obtained within the months of January, February and December 2010. The highest rain rates of 114.4 mm/hr, 114.2 mm/hr and 122.7 mm/hr was obtained between June and August of the years 2010, 2011 and 2012 respectively. For seasonal rain attenuation, the lowest value was 15.3dB in the driest months of January, February and December 2010. The highest rain attenuation (above 40dB) was gotten between June and August, followed by September to November season which recorded about 40dB in 2011 and 2012. March to May had an average attenuation value of about 35dB across the three years.

It could therefore be said that there would be more signal attenuation during the June to August season. Better signal quality will be experienced around December to February.

## 11. CONCLUSION

Rain rates and rain attenuation measurements for AKS using local data from the meteorology department of Uyo has been calculated for 99.999 to 99.9% availability of time. The refined Moupfouma model was used to obtain rain rate while the ITU-R P.618-11 model was used to obtain rain attenuation.

Table 4: Seasonal Variation of Rain Accumulation, Rain Rate and Rate Attenuation from 2010 to 2012

Month	2010			2011			2012		
	Rain Volume (mm)	Rain Rate (mm/h)	Rain Attenuation (dB)	Rain Volume (mm)	Rain Rate (mm/h)	Rain Attenuation (dB)	Rain Volume (mm)	Rain Rate (mm/h)	Rain Attenuation (dB)
Dec – Feb	10.5	24.7	15.3	86.0	46.2	23.8	488.6	77.4	33.3
Mar – May	273.5	65.2	29.9	818.0	90.3	36.7	540.0	79.8	34.0
Jun – Aug	1814.6	114.4	42.3	1803.4	114.2	42.3	2294.1	122.7	44.1
Sep – Nov	636.9	83.8	35.0	1261.4	102.7	39.7	1328.3	104.3	40.0

Results gotten show a high rain-rate and rain-attenuation for a tropical rain zone like Uyo, which was to be expected. Comparisons with related works carried out by two other people and ITU[4] show similar trends. These results will be useful in the preliminary design for both terrestrial and earth-satellite links. This is because a system will have to be designed with a fade margin above 48 dB. However, such a system might be very expensive; hence to be certain of the fade margin required, a reliable value of fade margin may be obtained through the analyses of a long-term data, such as a 7-year rainfall data. Furthermore, these analyses will provide a broad idea of rain attenuation to communication engineers for the design of link budget for improved signal propagation in this part of the Nigeria.

## 12. ACKNOWLEDGEMENT

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