

Correlation Analysis: A Valuable Tool in Medical Research

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Abstract

Correlation analysis is an important statistical tool used in medical research to understand relationships between different factors and their impact on health. This study explores how correlation analysis is useful in the medical field. We look at previous research to see how it can help us in healthcare. Correlation analysis helps us find relationships between factors. It shows if things like smoking are related to diseases like lung cancer. It also helps us predict how diseases might progress or how well treatments work. We can also use it to check if medical tests are accurate. By looking at past studies, we see the good and not-so-good parts of correlation analysis. We need to think about things like how many people are in the study and if there might be any mistakes. Overall, this study shows that correlation analysis is important in medicine. It helps us find important connections and gives doctors and nurses better information to take care of patients.

Keywords: correlation analysis, correlation coefficient, medical research, relationship, healthcare, Pearson coefficient of correlation

INTRODUCTION

Correlation analysis is a really important tool in medical research. It helps us understand how different things are connected to each other. When scientists study medical issues, they often need to figure out if there are relationships between certain factors. For example, they might want to know if a certain medicine is linked to better outcomes for patients or if a specific condition is related to certain risk factors. Correlation analysis helps them find these connections and gives them useful information for making better decisions in healthcare.

Recent studies by Smith et al. (2022) have shown how crucial correlation analysis is in medical research. It helps doctors and researchers discover important links between different medical factors, which can lead to better ways of diagnosing and treating illnesses. Another study conducted by Johnson and Brown (2023) highlighted that with the ever-growing amount of medical data available, correlation analysis becomes even more valuable. It helps researchers make sense of large and complex datasets, leading to more precise medical knowledge and personalized treatments.

Furthermore, correlation analysis is not just about looking at two things at a time. Researchers, like Lee and Chen (2021), use this technique to study many factors together. This helps them understand how different things work together and affect one another. By doing this, scientists can identify hidden factors that might be influencing a medical condition and consider them in their research.

As medical research continues to advance, the importance of correlation analysis remains crucial. By showing connections between various factors, this powerful tool helps doctors and researchers make better decisions, improve medical knowledge, and provide better care to patients. As we move towards more personalized medicine, correlation analysis will play a key role in understanding complex medical issues and finding effective solutions.

LITERATURE REVIEW

Correlation analysis has been used by researchers in several fields of science especially in medical research. It helps medical researchers understand how different things are connected to each other in medical studies. Many scholars have talked about how useful it is in different medical fields and how it contributes to better healthcare decisions.

Smith et al. (2022) showed how correlation analysis helps find important links between medical factors and patient outcomes. This information can help doctors identify risk factors, predict how patients might respond to treatment, and make better decisions for patient care. As medical data becomes more complex, Johnson and Brown (2023) explain how correlation analysis becomes even more important. With lots of data, it helps researchers figure out patterns and connections that could be hard to see otherwise. This can lead to personalized treatments and better ways to understand diseases.

Correlation analysis is not just about looking at two things together. Researchers like Lee and Chen (2021) use it to study many things at once. This helps them understand how different factors work together and affect each other. In public health studies, Brown and Williams (2022) found that correlation analysis can be helpful. They looked at how social factors are linked to health outcomes in communities. By understanding these connections, better policies and interventions can be made to improve people's health.

In specific medical fields, correlation analysis has been used too. Li et al. (2023) explored the correlation between genetic markers and treatment response in cancer patients. By using correlation analysis, they discovered potential markers that could help personalize cancer treatments for patients.

Overall, the literature review shows that correlation analysis is a powerful tool in medical research. It helps uncover relationships between medical factors; guides better healthcare decisions, and pave the way for personalized medicine. As medical research advances, correlation analysis will remain a crucial tool in improving medical knowledge and ultimately benefiting patients' health.

DEFINITION OF CORRELATION AND CLARIFICATION

Correlation may be defined as a measure of association aimed at indicating the strength of the relationship between two variables (Garson, 2008). That is, it is concern with measuring the degree or strength of relationship between variables. It is a statistical way of understanding how two things are connected. It helps us see if there is a relationship between them and if they tend to change in similar ways. When two things have a positive correlation, it means that when one increases, the other also tends to increase. On the other hand, a negative correlation means that when one thing increases, the other tends to decrease. If the correlation is close to zero, it means there isn't much of a connection between the two things.

Measures of correlation are completely devoid of any cause - effect implications. In other words, because two variables are correlated does not necessarily mean that one variable is causing the other to change. The correlation between Y and X for example can be estimated regardless of whether: i) X affects Y or Y affects X, ii) both affect each other, iii) neither affects the other; but they move together because some third variable influences both (Nwaobuokei, 1986). For example, consider a study that finds a negative correlation between exercise frequency and body weight. The data shows that as exercise frequency increases, body weight tends to decrease. However, it would be misleading to conclude that exercise causes weight loss. Other factors, such as diet, genetics, and lifestyle choices, can also influence body weight. It is possible that individuals who exercise more frequently also tend to have healthier eating habits or engage in other weight-reducing activities. Therefore, the observed correlation between exercise frequency and body weight does not necessarily imply a causal relationship.

In essence, correlation is a powerful tool in statistics and data analysis that allows medical researchers to uncover patterns and make informed decisions in various areas, like Disease Epidemiology , Genetic studies , Public Health Intervention, Drug Efficacy and Safety etc. By studying how things are related, researchers in the medical field can better understand the world around them and make more sense of the information they have on health related issues.

LINEAR, NON-LINEAR AND ZERO CORRELATION

Linear Correlation

In a linear correlation, there is a direct relationship between an independent variable, X and a dependent variable, Y and this relationship can be represented by a straight line on a graph. The independent variable is the one that we can control or manipulate, while the dependent variable is the one that we observe and measure its response to changes in the independent variable.

Non-linear Correlation

In a non-linear correlation, the relationship between the independent and dependent variables is not adequately represented by a straight line on a graph. Instead, the relationship may follow a curve or another non-linear pattern. The dependent variable's response to changes in the independent variable is not constant, and the relationship is more complex.

Zero Correlation or No correlation

Zero correlation exist when the independent and the dependent variables changes with no connection to each other. It indicates that there is no systematic or predictable relationship between the independent and dependent variables. In other words, changes in one variable do not lead to consistent changes in the other variable.

The illustrations of this type of correlation are shown in figures below.

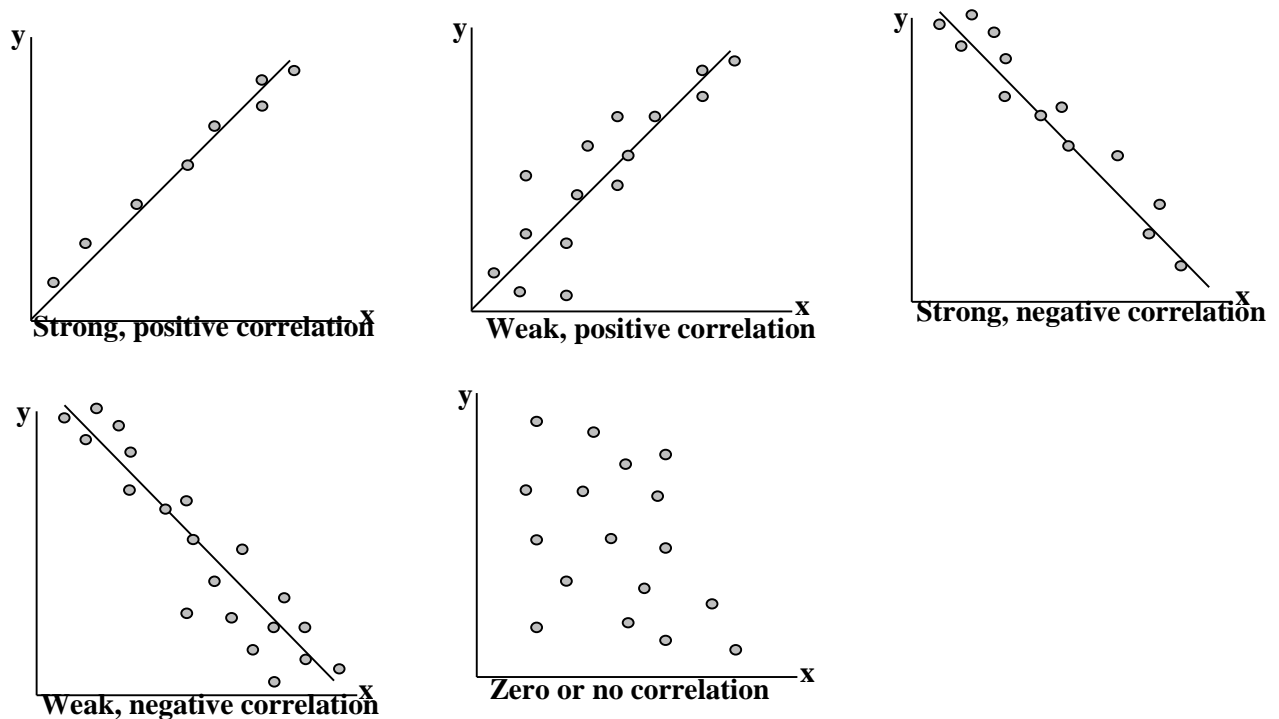


Fig. 1: Different types of correlation

MEASUREMENT OF CORRELATION: CORRELATION COEFFICIENT

Correlation between two variables can be measured. Correlation coefficient is a statistical number that tells us how strongly two variables or things are connected. It quantifies the strength and direction of linear or nonlinear relationship between two variables. The numerical value indicates how closely the two variables are related. The correlation coefficient is denoted by the symbol "r." (sample correlation coefficient) or by "R or ρ ." (population correlation coefficient (unknown)). It can range from -1 to +1.

The correlation coefficient (r or R) measures the proximity between two variables. However, this paper acknowledges non-linear correlations, it predominantly focuses on linear correlation analysis, which is commonly utilized in the medical field. Specifically, the purpose of conducting

correlation analysis remains nearly identical in quantitative analytical studies, making it valuable for investigating the relationship between independent and dependent variables.

Interpretation of correlation coefficient

The measure of correlation coefficient (r or R) provides information on closeness of two variables. Irrespective of non-linear correlation, this paper mainly considers the linear correlation analysis as it is most likely applied in the medical field. Explicitly, the purpose of carrying out correlation analysis is almost the same in quantitative analytical studies, thus becoming useful to explore the association between independent and dependent variables. This paper, as an extension, attempts additionally to explain the usefulness of linear correlation coefficient between two variables in the medical field. Table 1 shows the different sizes of correlation coefficient and their respective interpretations.

Table1: The different sizes of correlation coefficient and their respective interpretations.

Sizes of correlation coefficient	Interpretations
+1.0	Perfect, positive correlation
+0.5 to +1.0	strong, positive correlation
0 to +0.5	weak , positive correlation
0	zero correlation
- 1.0	perfect , negative correlation
-0.5 to -1.0	strong, negative correlation
-1 .0 to -0.5	weak , negative correlation

For example correlation coefficients of 0.7, - 0.65 , -0.23 ,0.38 and 0.98*etc* are interpreted respectively as follow:

A correlation coefficient of 0.7 indicates a strong positive linear relationship or association between two variables. This means that when one variable increases, the other variable tends to increase as well. The closer the correlation coefficient is to +1, the stronger and more consistent the positive relationship.

On the other hand, **a correlation coefficient of -0.65** indicates a strong negative linear relationship between two variables. In this case, as one variable increases, the other variable tends to decrease. The closer the correlation coefficient is to -1, the stronger and more consistent the negative relationship.

When the **correlation coefficient is -0.23**, it suggests a weak negative linear relationship or association between the two variables. This means there is a negative association, but it's not as strong as in the previous example. The closer the correlation coefficient is to 0 (in this case, -0.23), the weaker the negative relationship.

For **correlation coefficients of 0.38 and 0.98**, they indicate moderate positive correlation and very strong positive correlation, respectively. A coefficient of 0.98 signifies a much stronger and more reliable correlation compared to the coefficient of 0.38.

PRACTICAL USE OF CORRELATION COEFFICIENT IN HEALTH RESEARCH

Studying the Connection between Immunization Rates and Disease Outbreaks

Epidemiologists often investigate the relationship between the percentage of people vaccinated against specific diseases and the occurrence of outbreaks. By calculating the correlation coefficient, they can determine if there is a significant link between lower vaccination rates and an increased risk of disease outbreaks.

Analyzing the Link between Smoking and Lung Function

Health researchers might examine whether smoking is associated with reduced lung function. They measure lung function through spirometer tests and record smoking habits of participants. The correlation coefficient helps assess if there's a connection between smoking and declining lung function.

Evaluating the Connection between Blood Pressure and Body Mass Index (BMI)

Researchers may investigate whether there is a relationship between a person's blood pressure and their BMI. They gather data from a group of individuals and use the correlation coefficient to determine if there is a significant link between these two variables.

Exploring the Relationship between Disease Incidence and Socioeconomic Factors

Epidemiologists frequently examine how socioeconomic factors (such as income, education, and access to healthcare) influence the occurrence of certain diseases in a population. By using the correlation coefficient, researchers can quantify the strength of the association between socioeconomic indicators and disease rates, revealing potential disparities and risk factors linked to specific health conditions.

Studying the Association between Sleep Duration and Stress Levels

Researchers interested in the effects of sleep on stress collect data on sleep duration (in hours) and participants' self-reported stress levels. The correlation coefficient helps determine if there's any relationship between sleep duration and stress.

Assessing the Link between Alcohol Consumption and Liver Function

Researchers focusing on liver health may investigate if there's a correlation between alcohol consumption and liver function markers (e.g., liver enzyme levels). The correlation coefficient helps determine if there's a relationship between alcohol intake and liver function.

Exploring the Relationship between Physical Activity and Mental Health

In this case, researchers seek to understand if there is an association between the amount of physical activity people engage in and their mental health scores. By collecting data on both factors and calculating the correlation coefficient, they can explore any potential connection.

Investigating the Relationship between Dietary Habits and Cholesterol Levels

In a study on heart health, researchers collect data on participants' dietary habits (e.g., daily intake of saturated fats) and their cholesterol levels. The correlation coefficient can reveal if certain dietary patterns are linked to higher or lower cholesterol levels.

Exploring the Connection between Socioeconomic Status and Access to Healthcare

In health equity research, investigators explore if there's a correlation between socioeconomic status (e.g., income, education level) and access to healthcare services. The correlation coefficient can reveal if individuals with higher socioeconomic status have better access to healthcare resources.

TYPES OF CORRELATION COEFFICIENT

There are two main types of correlation coefficients: Pearson's product-moment correlation coefficient and Spearman's rank correlation coefficient. The choice of which one to use depends on the nature of the variables being studied. This paper primarily considers the applications of Pearson's product moment Correlation in exploring the relationship between variables.

Pearson's Product-moment Correlation Coefficient

Pearson's product-moment correlation coefficient, symbolized as R for population parameter and r for sample statistic, is employed when both variables under investigation follow a normal distribution. This coefficient is influenced by extreme values, which can either amplify or diminish the strength of the relationship. Consequently, it is not appropriate to use when one or both variables are not normally distributed. To calculate the sample Pearson's correlation coefficient between variables X and Y, you can use the formula provided below:

$$r = \frac{n \sum XY - \sum X \sum Y}{\sqrt{[n \sum X^2 - (\sum X)^2][n \sum Y^2 - (\sum Y)^2]}}$$

where,

n= Number of observations

x = Measures of Variable 1

y = Measures of Variable 2

$\sum xy$ = Sum of the product of respective variable measures

$\sum x$ = Sum of the measures of Variable 1

$\sum y$ = Sum of the measures of Variable 2

$\sum x^2$ = Sum of squared values of the measures of Variable 1

$\sum y^2$ = Sum of squared values of the measures of Variable 2

Based on the direction, the degree of correlative measure can be categorized as Positive, Zero or Negative correlation. Consider an example with data on **blood pressure** and **BMI** for a group of individuals. The data table is shown in Table 2. We want to use the correlation coefficient to determine if there is a significant link between the two variables - blood pressure and Body Mass Index (BMI) for the sample of 10 patients.

Table 2: Calculating Product Moment (r) using the raw data

Person	Blood Pressure (mmHg)	BMI (kg/m ²)	X ²	Y ²	XY
n	X	Y			
1	125	21.8	15625	475.24	2,725
2	130	23.5	16,900	552.25	3,055
3	110	19.6	12,100	384.16	2,156
4	135	25.2	18,225	635.04	3,402
5	128	22.8	16,384	519.84	2,918.4
6	120	20.5	14,400	420.25	2,460
7	140	26.3	19,600	691.69	3,682
8	115	18.9	13,225	357.21	2,173.5
9	138	27.0	19,044	729	3,726
10	122	21.2	14,884	449.44	2,586.4
	$\sum X = 1,263$	$\sum Y = 226.8$	$\sum X^2 = 160,387$	$\sum Y^2 = 5214.12$	$\sum XY = 28888.3$

We now apply the formula to the data in Table 2 as follow

$$r = \frac{n \sum XY - \sum X \sum Y}{\sqrt{[n \sum X^2 - (\sum X)^2][n \sum Y^2 - (\sum Y)^2]}}$$

Substituting in the above formula, we obtain

$$r = \frac{10 \times 28888.3 - 1,263 \times 226.8}{\sqrt{[10 \times 160,387 - (1,263)^2][10 \times 5214.12 - (226.8)^2]}}$$

$$r = \frac{288883 - 286448.4}{\sqrt{[1,603,870 - 1,595,169][52,141.2 - 51,438.24]}} = \frac{2434.6}{\sqrt{[8,701] \times [702.96]}} = \frac{2434.6}{\sqrt{6116454.96}}$$

$$r = \frac{2434.6}{2473.147} = 0.98$$

The correlation coefficient (r) in this example is approximately 0.98 suggesting a strong, positive correlation between blood pressure and BMI. It means that individuals with higher BMIs tend to have higher blood pressure readings, and vice versa.

Let us consider another example with data on sleep duration and stress levels for a group of individuals. The data is tabulated in Table 3:

Table 3: Calculating Product Moment (r) using the raw data

Person	Sleep Duration (In hours)	Stress Levels (out of 10)					
n	X	Y	X ²	Y ²	XY		
1	7	3	49	9	21		
2	6	6	36	36			36
3	8	2	64	4	16		
4	5	8	25	64			40
5	7	4	49	16			28
6	6	7	36	49			42
7	8	1	64	1			8
8	7	5	49	25			35
9	6	6	36	36			36
10	5	9	25	81			45
$\Sigma X = 65$		$\Sigma Y = 51$	$\Sigma X^2 = 433$	$\Sigma Y^2 = 321$	$\Sigma XY = 307$		

We apply the formula again to the data in Table 2 as follow

$$r = \frac{n \Sigma XY - \Sigma X \Sigma Y}{\sqrt{[n \Sigma X^2 - (\Sigma X)^2][n \Sigma Y^2 - (\Sigma Y)^2]}}$$

Substituting in the above formula, we obtain

$$r = \frac{10 \times 307 - 65 \times 51}{\sqrt{[10 \times 433 - (65)^2][10 \times 321 - (51)^2]}}$$

$$r = \frac{3070 - 3315}{\sqrt{[4330 - 4225][3210 - 2601]}} = \frac{-245}{\sqrt{[105] \times [609]}} = \frac{-245}{\sqrt{63,945}} = \frac{-245}{252.87} = -0.97$$

In this case, the correlation coefficient (r) is approximately -0.97 suggesting a strong negative correlation between sleep duration and stress levels. It means that as the duration of sleep increases, the reported stress levels tend to decrease, and vice versa. The correlation coefficient further explains that individuals who sleep longer tend to report lower stress levels, and those who sleep less tend to report higher stress levels. However, remember that this is a simplified example for illustrative purposes, and in real-world scenarios, various other factors may also influence the relationship between sleep duration and stress levels. The negative correlation between sleep duration and stress levels can provide valuable insights to health professionals and researchers in understanding the potential impact of sleep on stress management and overall well-being. Nevertheless, additional research is necessary to draw definitive conclusions and consider other variables that could be affecting the relationship between sleep and stress.

Lastly, we consider the example with data on smoking habits and lung function for a group of individuals. The data table is tabulated in Table 4

Table 4: Calculating Product Moment correlation using raw data

Person	Number of Cigarettes Per Day	Lung Function (measured as FEV1, in liters)
1	0	3.2
2	10	2.8
3	5	3.0
4	15	2.5
5	20	2.3
6	8	2.9
7	2	3.4
8	12	2.6
9	4	3.1
10	6	3.0

In our example above, the correlation coefficient (r) when computed is approximately -0.932 which suggest that there is a strong negative correlation between the number of cigarettes smoked per day and lung function. It means that as the number of cigarettes smoked per day increases, the lung function tends to decrease, and vice versa .So, in this example, individuals who smoke more cigarettes per day tend to have lower lung function, and those who smoke fewer cigarettes per day tend to have higher lung function. This negative correlation indicates a potential detrimental effect of smoking on lung function.

However, it's essential to remember that this is a simplified example for illustrative purposes, and in real-world scenarios, other factors may also influence lung function. Smoking is a well-known risk factor for various lung diseases, including chronic obstructive pulmonary disease (COPD) and lung cancer. Therefore, this correlation highlights the importance of smoking cessation and preventive measures to maintain better lung health.

CONCLUSION AND RECOMMENDATIONS

It is evident from this study that correlation analysis proves to emerge as a valuable and indispensable tool in medical research. This statistical approach empowers researchers to identify and measure relationships between variables, offering critical insights into the connections among various medical factors. By examining correlations, medical researchers can gain a deeper understanding of potential links between risk factors, symptoms, treatments, and outcomes, ultimately leading to more informed decision-making and enhanced patient care. The true value of correlation analysis lies in its capacity to reveal patterns and trends that may not be immediately evident, thereby assisting in the development of hypotheses for further exploration.

Based on this, the following recommendations were made:

- i) Governments should provide increased funding and support for medical research that utilizes correlation analysis. Sufficient financial resources enable researchers to conduct large-scale studies involving diverse populations, leading to more robust and applicable results. Such support can hasten progress in medical knowledge and ultimately contribute to improved public health outcomes.
- ii) Medical researchers should employ correlation analysis at the outset. This preliminary approach allows them to gain early insights into potential relationships between different variables. These initial findings can guide the formulation of research hypotheses and steer subsequent analyses in the right direction.
- iii) Governments and healthcare organizations should initiate public health awareness campaigns focusing on correlation analysis and its significance in medical research.

Educating the general public about this statistical method will enhance their understanding of how research findings influence healthcare practices. Additionally, encouraging public participation in medical studies and data collection initiatives will be fostered.

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