

**STUDY OF THE EXPERIMENTAL APPROACH OF THE RELATIVE LENGTH OF  
THE SURFACE ROLE OF THE HYDRAULIC JUMP EVOLVING IN  
RECTANGULAR CHANNEL OF SECTION COMPOSED WITH ROUGH BOTTOM**

W. Djamaa<sup>1\*</sup>, A. Ghomri<sup>2</sup>

<sup>1</sup>Laboratory of the exploitation and development of natural resources in arid zones, university of Ouargla. Department of Hydraulics and Civil Engineering University of Ouargla. Algeria

<sup>2</sup>Laboratory of Underground and Surface Hydraulics, University of Biskra, Department of Hydraulics and Civil Engineering University of El Oued. Algeria

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**ABSTRACT**

The aim of this experimental study is to analyze the relative length of the surface roll in a hydraulic jump evolving in a rectangular channel composed of a rough minor bed. We obtain a functional relationship, in non-dimensional terms, connecting the different characteristics of the jump.

**Keywords:** roughness, compound channel, rough background, hydraulic jump, rough minor bed, length of the surface roll.

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Author Correspondence, e-mail: [djamaa.walid94@gmail.com](mailto:djamaa.walid94@gmail.com)

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**1. INTRODUCTION**

Our study concerns the establishment of the empirical approach of the relative length of surface roll for a hydraulic jump controlled by a thin-walled threshold evaluating in a rectangular channel of composite shape with a rough minor bed. The bibliographic study



clearly shows that the fundamental dimensionless characteristics, intervening in the phenomenon of the hydraulic jump which evolves in a rectangular channel of compound form are the incident Froude number  $F_1$  or the volume flow  $Q$ , the upstream height  $h_1$  ( $h_1$  is the height at the foot of the jump), the downstream height  $h_2$  ( $h_2$  is the maximum height measured downstream of the jump) and the ratio  $L_r / h_1$  is the relative length of the surface roll of the hydraulic jump.

The primary objective of our experimental study is to develop purely empirical approaches to the relative length of the surface roller for a hydraulic jump evolving in a rectangular channel of a composed section with a rough bottom, thus to appear the effect of the roughness tested. experimentally on the characteristics of the hydraulic jump.

## 2. POSITION OF THE PROBLEM

The modification of the conditions upstream (flow, heights, ..... etc.) and downstream (a type of obstacle, its position, its height, ... etc.), Can lead to different configurations of a jump. The projection is said to be classic when it forms in a rectangular channel of little or no slope, without obstacle to the downstream. It is said to be controlled when its formation is conditioned by the installation of an obstacle downstream of the flow. It is said to be forced when it is formed on either side of the obstacle. The hydraulic jump can operate in prismatic or non-prismatic channels, with smooth or rough bottoms.

For our study which is presented is a hydraulic jump controlled by a thin-walled threshold which evolves in a rectangular channel of a composite section with a rough bottom with different openings  $h_1$  (photograph 1). Thus, for a fixed initial height  $h_1$ , several experimental measurements with different threshold heights and different relative roughnesses  $\varepsilon / b$  were obtained.

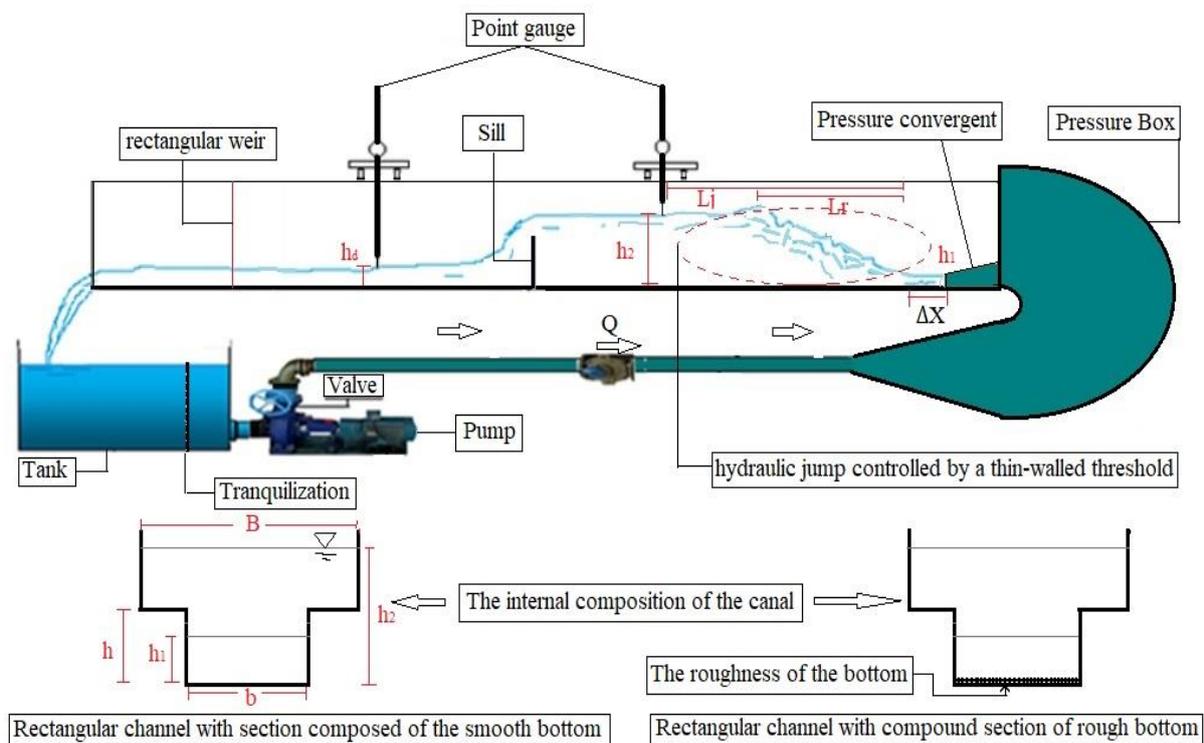
The hydraulic and geometrical characteristics interesting for our experimental study are the flow volume  $Q$  or number of incident Froude  $F_1$ , the height  $h_1$  of the incident flow, the final height  $h_2$  of the hydraulic jump, the relative length of surface roll  $L_r / h_1$  and the relative roughness  $\varepsilon / b$ . therefore the following dimensionless parameters:

- The number of Froude  $F_1$  such as:  $F_1 = Q / (gb^2 h_1^3)$

- The ratio  $L_r / h_1$  of the relative length of a surface roll of the hydraulic jump in the minor bed.
- The ratio  $L_r / h_1$  of the relative length of a surface roll of the hydraulic jump in the major bed.

### 3. DESCRIPTION OF THE TESTS

The experimental of hydraulic jump controlled by a thin-walled sill in a rectangular channel with a rough bottom were made at the Laboratory for the exploitation and development of natural resources in arid zones (EVRNZA) of the Department of Civil and Hydraulic Engineering of the University of Ouargla. The bottom of the canal is perfectly horizontal (with no slope). A supply basin is connected to the channel by means of a circular pipe 150 mm in diameter. This is connected to a closed metal box, on which is inserted an opening with a flat sheet metal wall of determined width opening into the channel. The role of this wall is to generate an incident flow at high speed. The outlet section is variable and its height will correspond to the initial height  $h_1$  of the hydraulic jump. The volume flows are adjusted by manipulating the valve. The channel is supplied by a pump delivering up to 55.55 l / s.



**Fig.1.** Schematic definition of the hydraulic jump controlled by a thin-walled continuous

threshold in a rectangular channel with a composite section with a rough bottom.



**Photograph 1.** the formation of the surface roll length for a hydraulic jump in a rectangular channel of a compound section with a rough bottom.

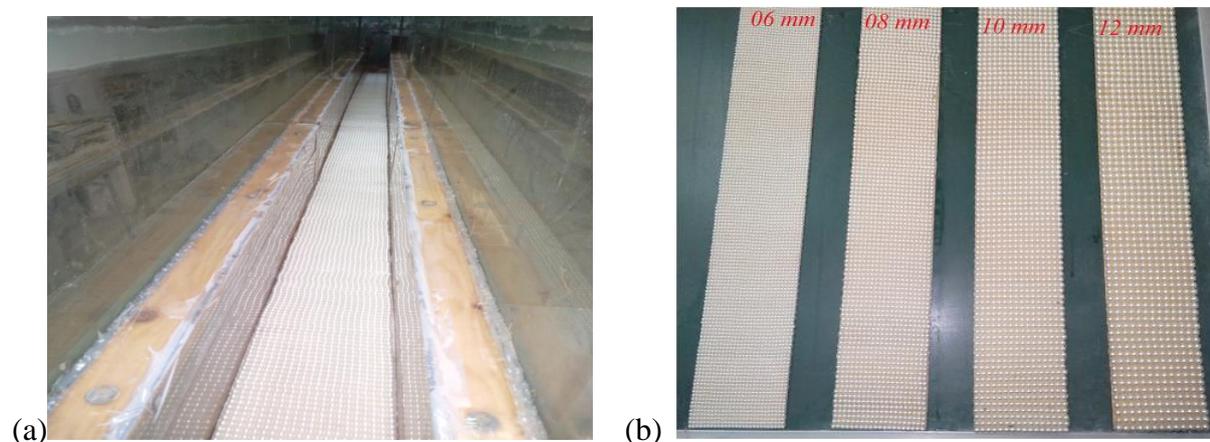
The experiment was conducted under five initial heights of flow:  $h_1$  (cm) = 2; 2.5; 3; 3.5 and 4. The formation of the controlled hydraulic jump is conditioned by the establishment of a threshold downstream of the flow. We used thresholds of different heights (2.5 cm to 21 cm) for the formation and control of the hydraulic jump (**Photograph 2**).



**Photograph 2.** Thin-walled thresholds 2.5 à 21 cm

Concerning the rough bottom of the channel, we tested various roughnesses which are imposed on the bottom of the channel of a compound section, we proceeded the following stages:

1. We stuck plastic balls on a carpet in a linear and regular way, on 4 meters of the test channel.
2. The rough carpet obtained is then carefully glued to the minor bed of the rectangular channel of the composite section.
3. The roughnesses obtained are  $\varepsilon=06$  mm,  $\varepsilon=08$  mm,  $\varepsilon=10$  mm et  $\varepsilon=12$  mm



**Photograph 3.** (a): Photograph of a rough carpet carefully glued to the bottom of the rectangular channel of composite section. (b): Photograph of the four rough carpets:  $\varepsilon = 06$  mm,  $\varepsilon = 08$  mm,  $\varepsilon = 10$  mm and  $\varepsilon = 12$  mm.

So when we obtain a configuration of the controlled hydraulic jump, we perform, for an initial height  $h_1$  and a fixed threshold position  $x$ , the following operations:

1. Reading of the overflow height  $h_{dev}$  of the rectangular overflow.
2. Calculation of the corresponding volume flow, by applying the relationship of the rectangular flow meter (HachemiRachedi L.2006):

$$Q = 0,3794 \sqrt{2g} \beta (1 + 0,16496 \beta^{2,0716})^{3/2} h_{dev}^{3/2} \quad [1]$$

With:

Q: the flow in (m<sup>3</sup> / s);

$\beta = b / B$ : Ratio of the enlargement. ;

b: width of the notch (m). ; B: the width of the channel (m). ;

$g$ : the acceleration of gravity ( $m/s^2$ );

$h_{dev}$ : The height of the overhanging blade in (m).

3. Calculation of the Froude number  $F_1$  of the incident flow, by applying the relation [1].

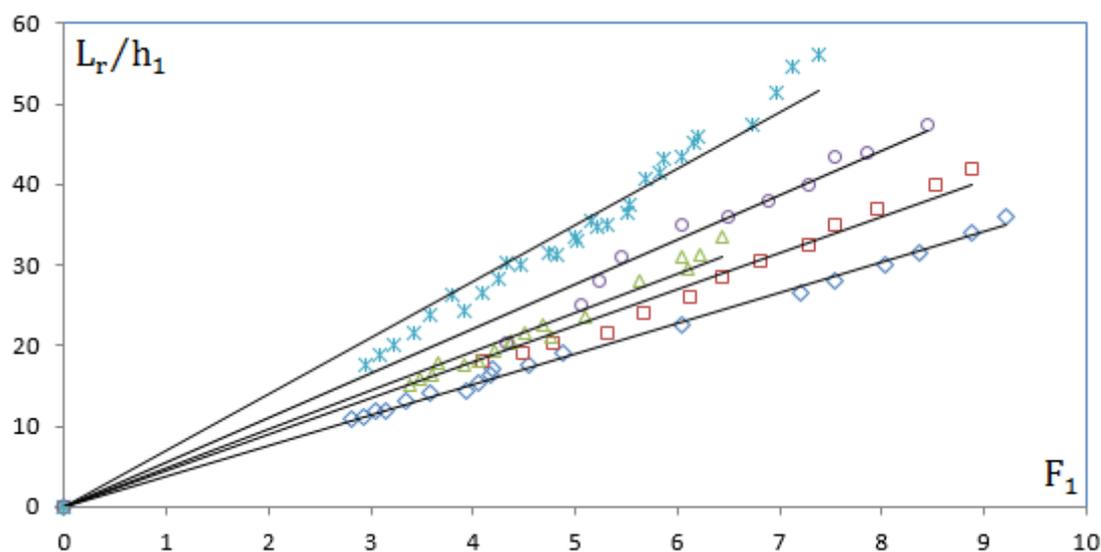
4. Measurement of the final height  $h_2$  of the hydraulic jump.

## 4. RESULTATS EXPERIMENTAUX

### 4. 1. Variation of the relative length of surface roller $L_r / h_1$ as a function of the Froude number $F_1$ in the minor bed.

The relative length of the surface roll is the distance from the start of its formation to its end. Figure 2 shows the variation of the relative length of the surface roller  $L_r / h_1$  as a function of the Froude number for five values of absolute roughness:  $\varepsilon = 00$  mm;  $\varepsilon = 06$  mm;  $\varepsilon = 08$  mm;  $\varepsilon = 10$  mm and  $\varepsilon = 12$  mm in the minor bed. There are thus five-point clouds, where each depends on a well-defined absolute roughness.

Furthermore, the analysis of the experimental measurement points of the hydraulic jump with a rough bottom, shows that for each roughness value " $\varepsilon$ " tested corresponds a linear type curve of the form  $L_r/h_1 = a_1(F_1)$ .



**Fig.2.** Variation of the relative length of the surface roll  $L_r / h_1$  as a function of the Froude number  $F_1$ , for five different roughnesses " $\varepsilon$ " ( $\square$ ) 12 mm ;( $\square$ ) 10 mm; ( $\Delta$ ) 08 mm; (O) 06 mm and (\*) 0 mm. (—) Adjustment curves

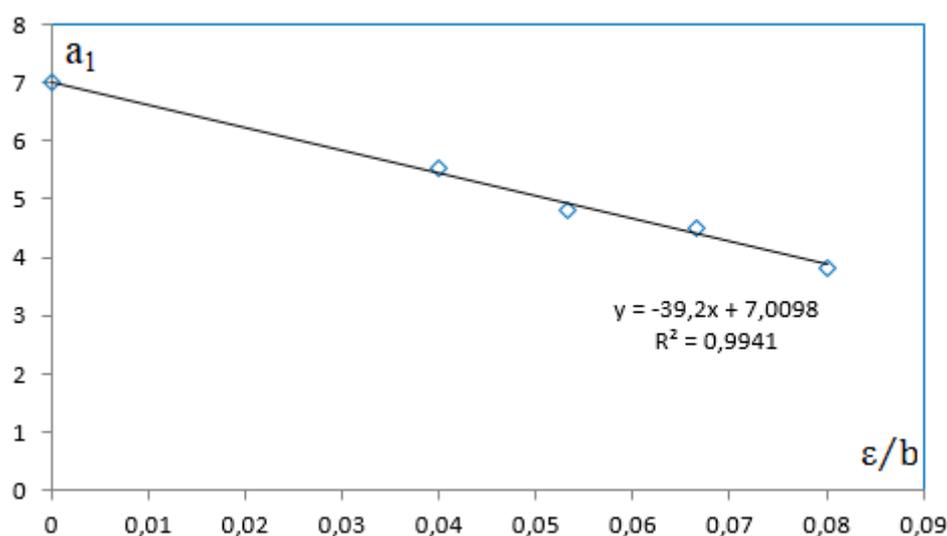
Analysis of these results shows that the relative length  $L_r / h_1$  increases as the number of

Froude  $F_1$  also increases and this for all roughness. In addition, the relative increase in roughness  $\varepsilon / b$  causes the decrease in the ratio of the relative length  $L_r / h_1$ , this is due to the roughness of the bottom of the channel which generates the compactness of the hydraulic jump.

Table 1 groups the values of the coefficient  $a_1$ .

**Table 1.** Coefficients  $a_1$  of the adjustment curves

$\varepsilon/b$	$a_1$	R2
0,08	3,817	0,995
0,06666667	4,501	0,985
0,05333333	4,809	0,976
0,04	5,528	0,983
0	6,986	0,966



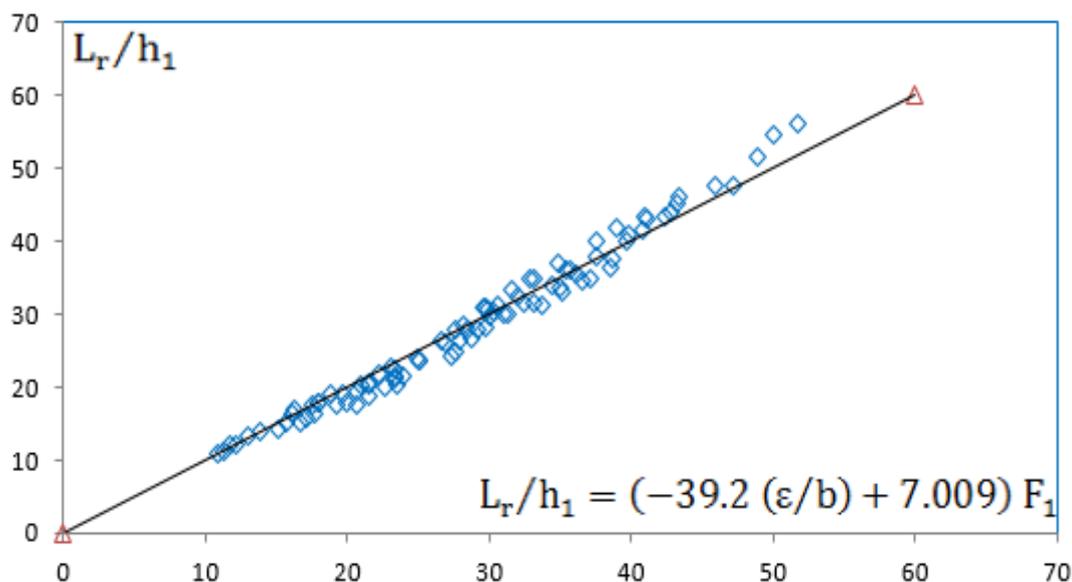
**Fig.3.** Variation of the coefficient " $a_1$ " as a function of the relative roughness  $\varepsilon/b$  in the minor bed

The adjustment of the couples of values ( $a_1$ ,  $\varepsilon/b$ ) of table 1 made it possible to arrive with a good correlation according to the following linear relation:  $a_1 = -39,2 \cdot \varepsilon/b + 7,0098$ , with  $R^2 = 0,9941$ . This equation is presented in Figure 3. The equation linking the upstream relative length of the surface roll  $L_r / h_1$ , the Froude number  $F_1$  and the relative roughness  $\varepsilon/b$  are then written:

$$L_r / h_1 = (-39,2 * \varepsilon / b + 7,0098) F_1 \quad [2]$$

With  $0 \leq \varepsilon / b \leq 0.8$

Figure 4 also shows that the relation  $L_j / h_1 = f(\varepsilon / b, F_1)$  adjusts with a good correlation for the minor bed in majorities of the experimental measurement points and these follow perfectly the first bisector.



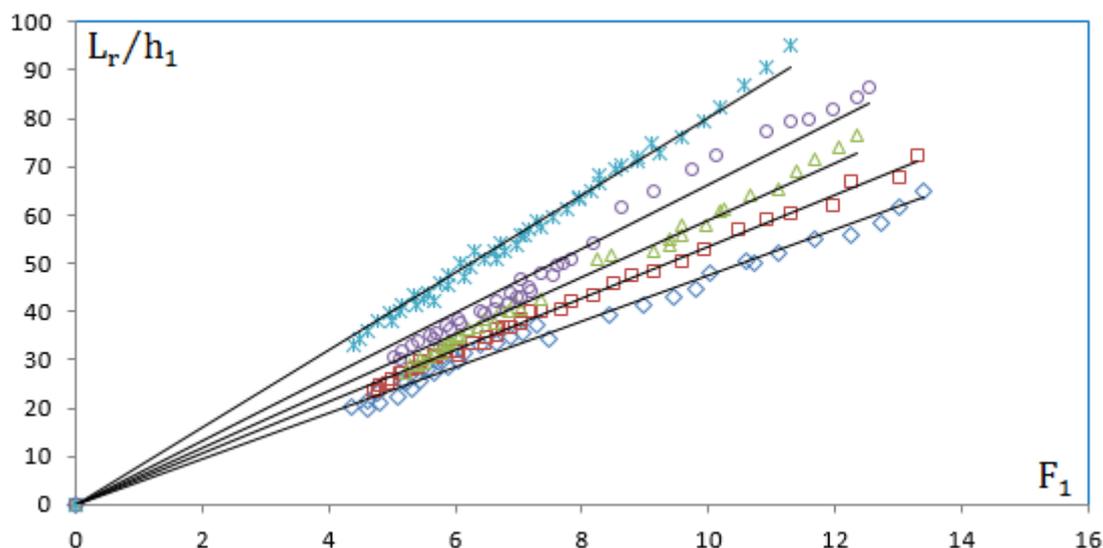
**Fig.4.** Variation of the relative length of the surface roll  $L_r / h_1$  as a function of  $f(\varepsilon / b, F_1)$ .

(□) The experimental points of the controlled jump with a rough bottom. (—) First bisector

#### 4.2 Variation of the relative length of the surface roll $L_r / h_1$ as a function of the Froude number $F_1$ in the major bed.

As we did with the minor bed, we have plotted the graph of the variation  $L_r / h_1$  as a function of the Froude number  $F_1$  for five values of absolute roughness in the major bed. There are also five-point clouds, each of which depends on a specific roughness.

Furthermore, the analysis of the experimental measurement points of the hydraulic jump with rough bottom for the major bed, also shows that for each roughness value " $\varepsilon$ " corresponds a linear type curve of the form  $L_r / h_1 = a_2(F_1)$ .



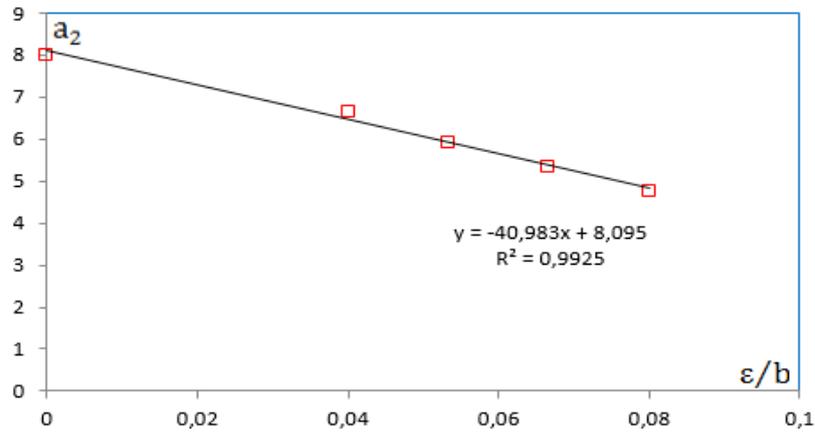
**Fig.5.** Variation of the relative length of the surface roll  $L_r / h_1$  as a function of the Froude number  $F_1$ , for five different roughness " $\epsilon$ " :( $\square$ ) 12 mm ;( $\square$ ) 10 mm; ( $\Delta$ ) 08 mm; (O) 06 mm and ( $*$ ) 0 mm. (—) Adjustment curves

The analysis of these curves shows that the relative length of the surface roll  $L_r / h_1$  increases with the increase in the number of Froude  $F_1$  and this for all the roughnesses tested. In addition, the relative roughness  $\epsilon / b$  increases with the decrease in the ratio of the relative length of the surface roll  $L_r / h_1$ , this is due to the roughness of the bottom of the channel, which causes energy dissipation.

Table 2 groups the values of the coefficient  $a_2$ .

**Table 2.** Coefficients  $a_1$  of the adjustment curves

$\epsilon/b$	$a_2$	$R^2$
0,08	4,744	0,989
0,06666667	5,346	0,996
0,05333333	5,899	0,987
0,04	6,642	0,973
0	8,008	0,992



**Fig.6.** Variation of the coefficient "  $a_2$ " as a function of the relative roughness  $\epsilon / b$  in the major bed

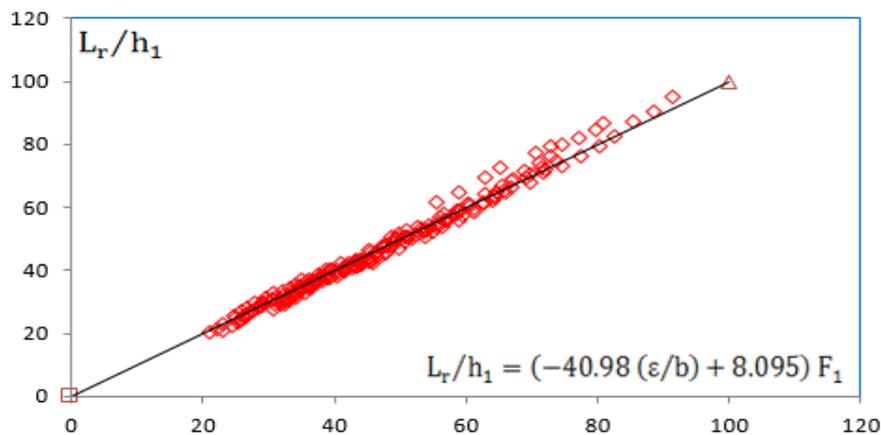
Adjustment of value pairs ( $a_2, \epsilon / b$ ) of Table 6 made it possible to arrive with a good correlation to the following linear relationship:  $a_2 = -40.983 (\epsilon / b) + 8.095$ .

The equation linking the upstream relative length of the surface roll  $L_r / h_1$ , the Froude number  $F_1$  and the relative roughness  $\epsilon / b$  for the major bed is written as follows:

$$L_r / h_1 = (-40.983 * (\epsilon / b) + 8.095) F_1 \tag{3}$$

With  $0 \leq \epsilon/b \leq 0.8$

Figure 7 also shows that the relation  $L_r / h_1 = f(\epsilon / b, F_1)$  adjusts with a good correlation for the major bed in the majority of the points of experimental measurements, and these last perfectly follow the first bisector.

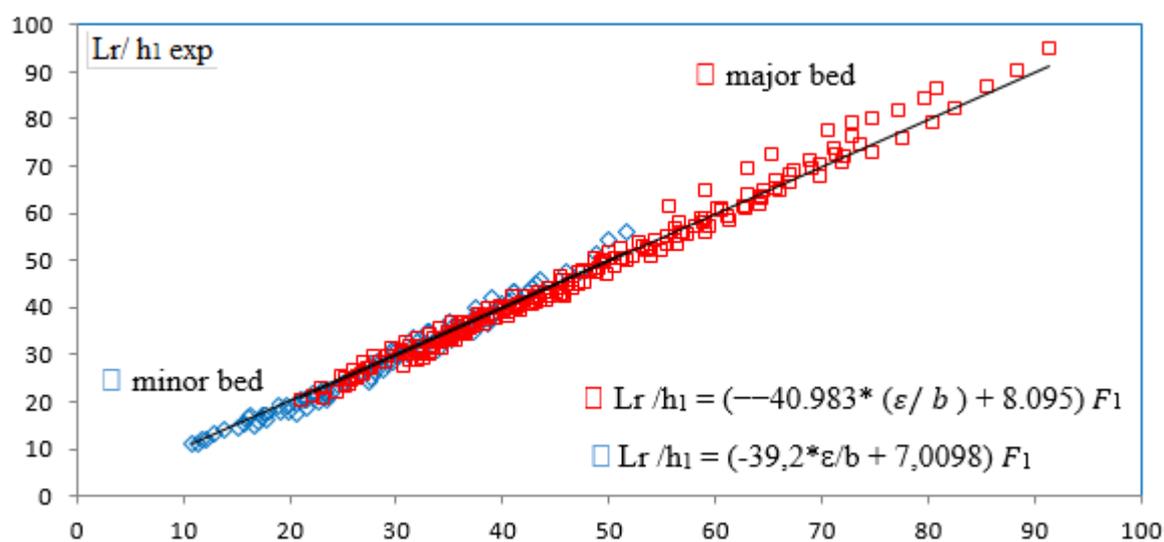


**Fig.7.** Variation of the relative length of the surface roll  $L_r / h_1$  experimental as a function of  $f(\epsilon / b, F_1)$ . (□) The experimental points of the controlled projection with a rough bottom in the major bed. (—) First bisector

Figure 8 shows the variation of the experimental relative length of the surface roll  $L_r / h_1$  as a function of  $f(\varepsilon / b, F_1)$  for the compound section.

This figure shows the comparison between experimental measurements of the relative length of the surface roll  $L_r / h_1$  with their global relationships obtained for the two beds of the component.

We deduce that the compound section presents a reduction in the relative length of the surface roll  $L_r / h_1$  of the hydraulic jump in the minor bed than that in the major bed.



**Fig.8.** shows the variation of the experimental relative length of the surface roll  $L_r / h_1$  as a function of  $f(\varepsilon / b, F_1)$  for the two cases ( $\square$  minor bed;  $\square$  major bed)

It is concluded that the composite section of the rectangular channel has a positive effect reducing the relative length of the surface roll in the minor bed than that in the major bed.

## 6. CONCLUSION

From the tests and results obtained at the laboratory level, it appears that the effect of roughness appears clearly on the characteristics, this type of hydraulic jump studied against the effect of the opening  $h_1$  no longer appears on their characteristics.

Initially, the study was interested in the variation of the relative length of surface roll  $L_r / h_1$  according to the number of Froude  $F_1$  for five different openings and five roughness tested experimentally for the two beds of the channel experimentation. Secondly, we note that the

increase in the number of Froude  $F_1$  leads to that of the relative length of the surface roll of the hydraulic jump  $L_r / h_1$  for the two beds of the channel. Furthermore, for the same number of Froude  $F_1$ , the relative length of the surface roller  $L_r / h_1$  diminishes with the increase in the relative roughness  $\varepsilon / b$  imposed on the bottom of the experimental channel.

we can conclude that for a range of Froude numbers and different roughness tested, the hydraulic jump in a rectangular channel of a compound section, presents two global experimental approaches  $L_r / h_1 = f(F_1, \varepsilon / b)$  by which could be used in the design of ancillary works such as the sinking basin.

**Finally, one could judge that the hydraulic jump evolving in a rectangular channel of a section composed of the rough font has a reducing effect on the characteristics of the flow in minor bed more than the major bed.**

#### MAIN RATINGS

b width of the minor channel bed [m]

B Width of the major bed [m]

$F_1$  Number of Froude upstream of the hydraulic jump [ ]

g Acceleration of gravity [m / s]

$h_1$  Initial height of the projection [m]

$h_2$  Final height of the projection [m]

h Full edge height of minor bed [m]

$L_r$  length of the surface roll of the hydraulic jump [m]

$L_r / h_1$  Relative length of the surface roll of the hydraulic jump [ ]

Q Volume flow [ $m^3/s$ ]

$\varepsilon$  Absolute roughness [m]

$\varepsilon / b$  Relative roughness [ ]

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